



Viva Number Lines!

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Permission granted to educators to copy game boards for classroom use.

Build a Number Track

- Take a cube away and ask a friend to name the missing number.
- What number do you land on if you start at 5 and jump on 2 more?
- Turn over every second cube. Read the numbers.



Build a Number Track

- Put a finger on 5, put another finger on 7. What number comes between 5 and 7?
- Break apart all the cubes and put the numbers in order.
- What number comes just after five?



Break it Down

2 players

Adding on a number chart

Purpose

In this game, students practice adding two-digit numbers by breaking up one addend into tens and ones. A partially-filled number chart is used to help the students add the tens and then the ones. For example, to calculate $443 + 24$, the students are encouraged to think, $443 + 20 + 4$.

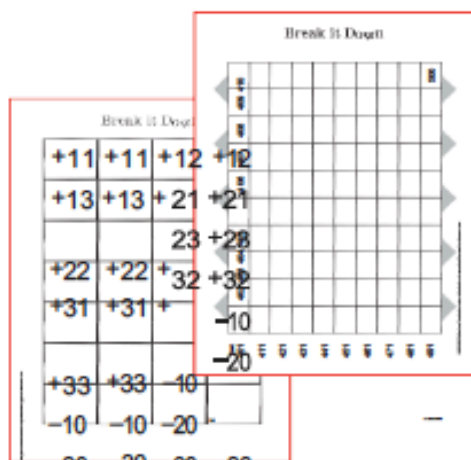
Materials

Each pair of players will need

- A 'Break it Down' game board (page 14) as shown below.
- One (1) set of operation cards. Copy page 15 as shown below. Cut out and laminate the cards to make one set.

Each player will need

- One (1) transparent counter (a different color for each player).



How to Play

The aim is to reach or pass 500 on the game board.

- The operation cards are shuffled and placed face down in a stack.
- The players place their counters in the 'Start' position (401) on the game board.
- The first player draws the top card. If an addition card is drawn, the player moves his or her counter that number of spaces forward on the game board.

Example: Michelle draws '+ 32' and moves her counter down three rows (+ 30) and two spaces to the right (+ 2).

- Initially, if a subtraction card is drawn, the player remains at 'Start'. Throughout the game, if a subtraction card is drawn, the player moves his or her counter back that number of spaces.

Example: James draws '- 30' and moves his counter up three rows (- 30).

- If a subtraction card would result in a score less than 401, the player returns his or her counter to 'Start'.
- The card is placed at the bottom of the stack.
- The other player has a turn.
- The first player to reach or pass 500 is the winner.

Reading the Research

Although more abstract, a partially-filled hundred chart works better to activate mental strategies than the easier filled-in chart that is often used in classrooms

Before the Game

Show a transparency of the game board on the overhead projector. Place a transparent counter on 423. Select an addition card, such as '+ 31', and ask students to figure out the sum. Encourage them to explain their thinking. Can the students see they need to move the counter down three rows and one space to the right? Do they know this is the same as adding 30, then adding 1? Discuss alternative strategies, such as adding the ones first, then the tens.

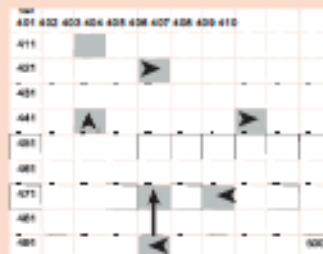
During the Game

At various stages of the game, ask students how many more they need to make 500. Encourage them to share how they figured out the answer. The discussion will vary, but they should see that one efficient strategy is to build the ones to the next multiple of ten and then figure out the number of tens they need to get to 500. For example, if a player has a counter on 472, he or she will need 8 more to make 480 and 20 more to make 500, so the player needs a total of 28. Alternatively, they could count forward in tens and then build the ones to 500.

After the Game

Draw arrows on an overhead transparency of the game board as shown. Tell the students that the arrows represent numbers that have been added or subtracted. The shaded areas indicate the starting numbers and the answers. Have the students figure out the numbers that have been added or subtracted each time.

Afterwards, give the students a copy of the game board. As cards are drawn, they could draw arrows to show how to add or subtract the two-digit number, before shading the box that would show the answer.



| | | | |
|-----|-----|-----|-----|
| | | | |
| -11 | -11 | -12 | -12 |
| -13 | -13 | -21 | -21 |
| -22 | -22 | -23 | -23 |
| -31 | -31 | -32 | -32 |
| -33 | -33 | +10 | +10 |
| +10 | +10 | +20 | +20 |
| +20 | +30 | +30 | +30 |

Beyond the Game

- The students can play the same game using different target numbers, such as 200, 300, or 450. They will need to make a new game board for each new target number. The same set of operation cards can be used.
- The students could play a subtraction version of 'Break it Down'. Make a new set of cards as shown. In this game, the students start on 500 and race backwards to 401.

| Start 401 | 402 | 403 | 404 | 405 | 406 | 407 | 408 | 409 | 410 |
|--------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 411 | | | | | | | | | |
| 421 | | | | | | | | | |
| 431 | | | | | | | | | |
| 441 | | | | | | | | | |
| 451 | | | | | | | | | |
| 461 | | | | | | | | | |
| 471 | | | | | | | | | |
| 481 | | | | | | | | | |
| 491 | | | | | | | | | 500 |

Break it Down

| | | | |
|-----|-----|-----|-----|
| +11 | +11 | +12 | +12 |
| +13 | +13 | +21 | +21 |
| +22 | +22 | +23 | +23 |
| +31 | +31 | +32 | +32 |
| +33 | +33 | -10 | -10 |
| -10 | -10 | -20 | -20 |
| -20 | -30 | -30 | -30 |

Leaps and Bounds

Using number lines to calculate difference

2 or 3 players

Purpose

In this game, students calculate the difference between a pair of two-digit numbers. The numbers do not require the students to bridge across a ten.

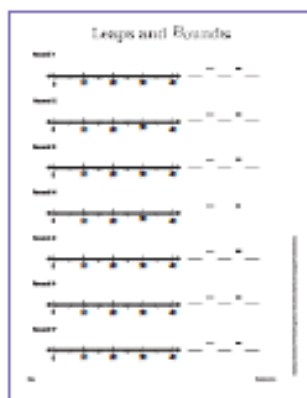
Materials

Each group of players will need

- Two (2) number cubes made from blank wooden cubes. One cube (Cube A) should show the numerals 25, 27, 29, 35, 36, and 38. The second cube should show numerals 10-15.

Each player will need

- A 'Leaps and Bounds' game board (page 14) as shown below.



How to Play

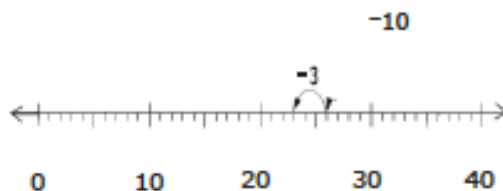
The aim is to achieve the greater difference.

- The first player rolls the number cubes.
- Using the two numbers, the player writes a subtraction sentence in the first round on his or her game board.

Example: Beth rolls 13 and 36, and writes $36 - 13 = \underline{\quad}$.

- The player mentally calculates the answer and writes it in the number sentence, then uses the number line to show his or her thinking.

Example: Beth writes $36 - 13 = 23$ and shows how she starts with 36, counts back 10, then 3.



- The other player(s) has a turn.
- The player with the greater difference (answer) scores a point for the round. This is indicated with a ✓.
- The player with the greater number of points after seven rounds is the winner.

Reading the Research

Research shows that children need many different kinds of number experiences to help them deal with real-life situations. It is important that they work regularly with a variety of number representations, including a counting model, a linear model such as a number line, a place value model and a quantity model (Irons, 2002).

Before the Game

Draw a number line on the board, like the ones shown on page 12. Invite a volunteer to roll the number cubes and write a subtraction sentence. Encourage the students to picture in their heads the jumps they would make to calculate the answer. Call upon one student to draw the jumps and explain his or her strategy. Repeat this activity several times before explaining the rules of the game.

During the Game

Observe the various strategies that different students use to calculate the answers. At a later stage, call upon these students to share their methods with the entire class. For example, to calculate $29 - 14$, the students may count back 10 then count back 4, or vice versa. Alternatively, they may change the two numbers by thinking, $29 - 14$ is the same as $30 - 15$.

After the Game

Draw another number line on the board. Share stories that involve all three models of subtraction. At this stage, make sure they do not involve bridging across a ten, for example

Take away: *A school bus was carrying 37 students. Twelve students got off. How many students were left on the bus? (25 students.)*

Missing addend: *Jemma needs \$29 to buy a gift. She has saved \$14. How much more money does she need to save? (\$15.)*

Comparison/difference: *Andy planted 26 trees in the morning and 15 trees in the afternoon. How many more trees did he plant in the morning than the afternoon? (11 more trees.)*

For each problem, invite volunteers to draw jumps on the number line to explain how they would calculate the answer mentally. Did all students use the same strategy for all three models of subtraction? Did any one strategy better suit a particular model?

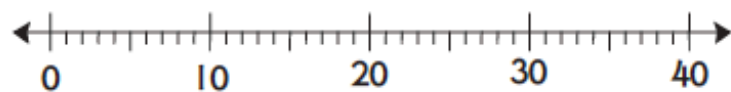
Beyond the Game

- Extend the game by changing Cube A. Make a new cube using the numerals 37, 38, 39, 45, 47, and 49. Each player will also need a copy of the 'Leaps and Bounds Again' game board on page 15 (illustrated).
- Change Cube A again to show the numerals 22, 23, 24, 31, 32, and 33. This will require the students to bridge across a ten. Either game board can be used.



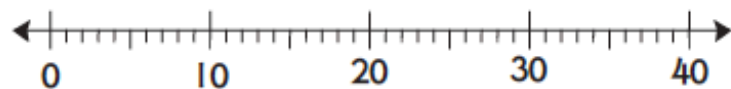
Leaps and Bounds

Round 1



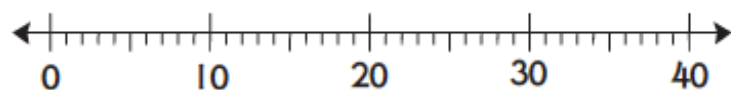
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Round 2



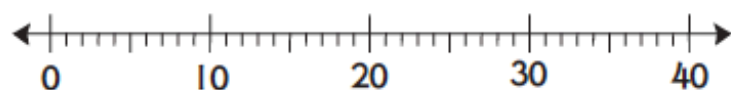
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Round 3



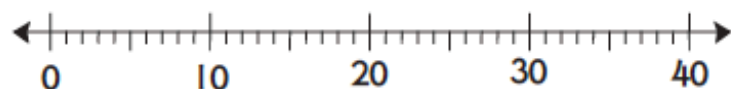
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Round 4



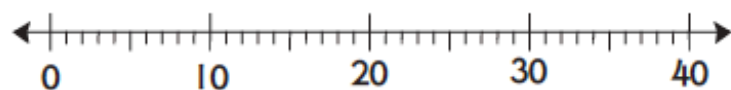
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Round 5



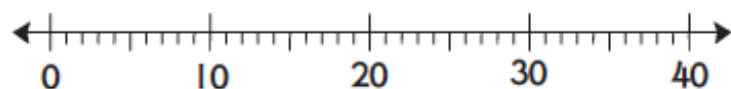
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Round 6



— — — — —
— — — — —
— — — — —

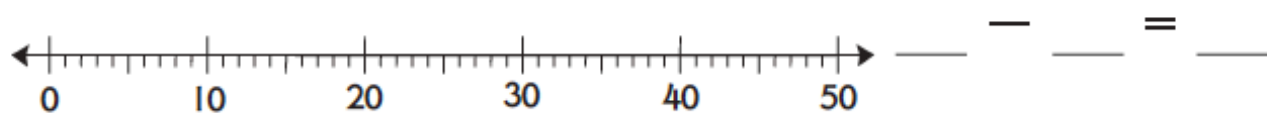
Round 7



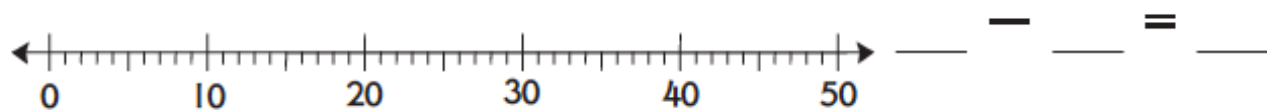
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Leaps and Bounds Again

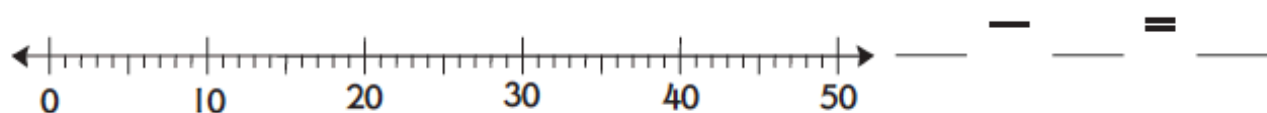
Round 1



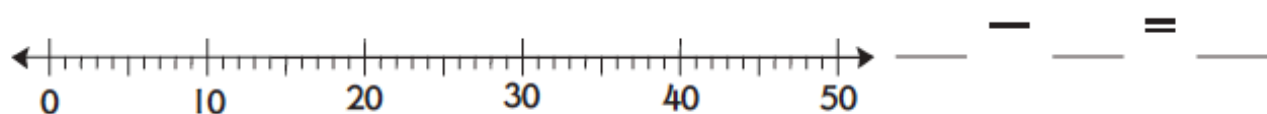
Round 2



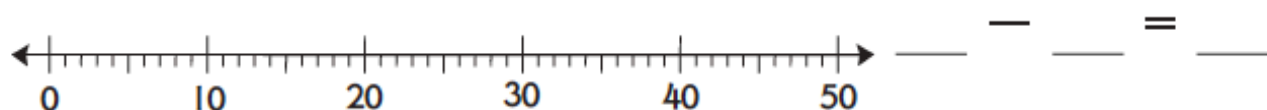
Round 3



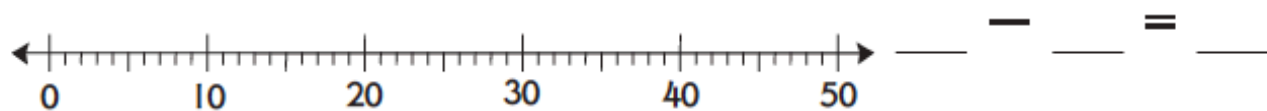
Round 4



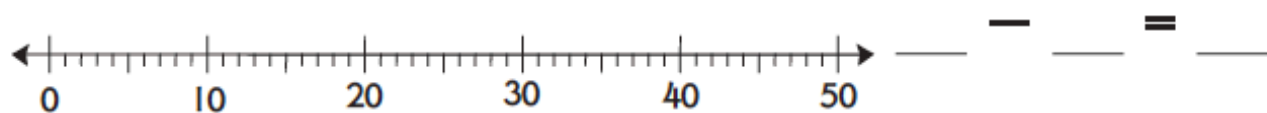
Round 5



Round 6



Round 7



Jump Back

Using number lines to calculate difference

2 or 3 players

Purpose

In this game, students calculate the difference between two- and three-digit numbers. The numbers involved do not require the students to bridge across a ten or hundred. The extension activity requires the students to subtract decimal fractions involving tenths.

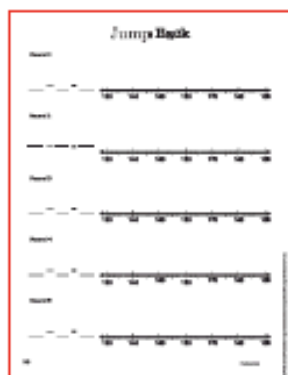
Materials

Each group of players will need

- Two (2) number cubes made from blank wooden cubes. One cube should show the numerals 166, 167, 177, 178, 188, and 189. The second cube should show the numerals 23, 24, 25, 33, 34, and 35.

Each player will need

- A 'Jump Back' game board (page 18) as shown below.



How to Play

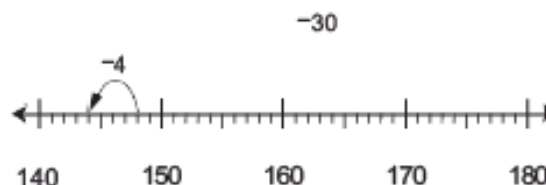
The aim is to achieve the greater difference.

- The first player rolls the number cubes.
- Using the two numbers, the player writes a subtraction sentence in the first round on his or her game board.

Example: Silas rolls 34 and 178. He writes $178 - 34 = \underline{\quad}$.

- The player mentally calculates the answer and writes it in the number sentence, then uses the number line to show his or her thinking.

Example: Silas writes $178 - 34 = 144$ and shows how he starts with 178, counts back 30, then 4.



- The other player(s) has a turn.
- The player with the greater difference (answer) scores a point for the round. This is indicated with a ✓.
- The player with the greater number of points after five rounds is the winner.

Reading the Research

Research shows that children need many different kinds of number experiences to help them deal with real-life situations. It is important that they work regularly with a variety of number representations, including a counting model, a linear model such as a number line, a place-value model and a quantity model (Irons, 2002).

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Before the Game

Draw a number line on the board, like the ones shown on page 18. Invite a volunteer to roll the number cubes and write a subtraction sentence. Encourage the students to picture in their heads the jumps they would make to calculate the answer. Call upon one student to draw the jumps and explain his or her strategy. Repeat this activity several times before explaining the rules of the game.

During the Game

Observe the various strategies that different students use to calculate the answers. At a later stage, call upon these students to share their methods with the entire class. For example, to calculate $169 - 24$, the students may count back 20 then count back 4, or vice versa. Alternatively, they may change the two numbers by thinking, $169 - 24$ is the same as $170 - 25$.

After the Game

Draw another number line on the board. Share stories that involve all three models of subtraction. At this stage, make sure they do not involve bridging across a ten, for example

Take away: *A truck was loaded with 175 crates. At the first stop, 23 crates were delivered. How many crates were left on the truck? (152 crates.)*

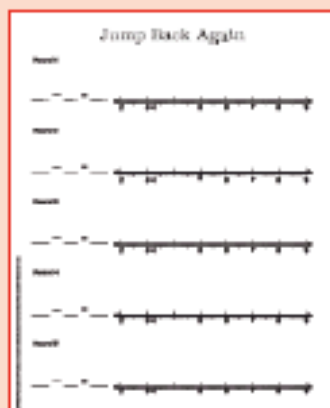
Missing addend: *Hazel needs \$188 to buy a new bike. She has saved \$35. How much more money does she need to save? (\$153.)*

Comparison/difference: *Grant sold 32 ice-creams before lunch and 167 ice-creams after lunch. How many more ice-creams did he sell in the afternoon than the morning? (135 ice-creams.)*

For each problem, invite volunteers to draw jumps on the number line to explain their mental strategies. Did all students use the same strategy for all three models of subtraction? Did any one strategy better suit a particular model?

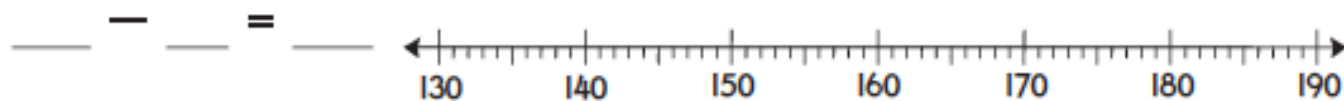
Beyond the Game

The game can be extended to involve tenths. Make two new number cubes by writing the numerals 7.7, 7.8, 7.9, 8.7, 8.8, and 8.9 on the faces of one cube and 3.2, 3.3, 4.3, 4.4, 5.4, and 5.5 on the faces of another blank cube. Each player will also need a copy of the 'Jump Back Again' game board on page 19 (illustrated). The rules of the game are the same.

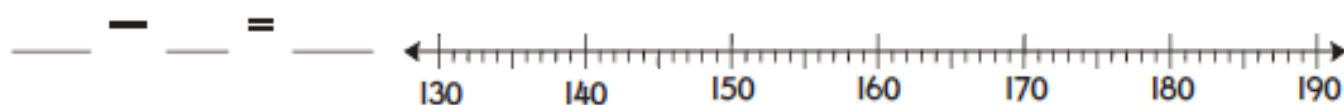


Jump Back

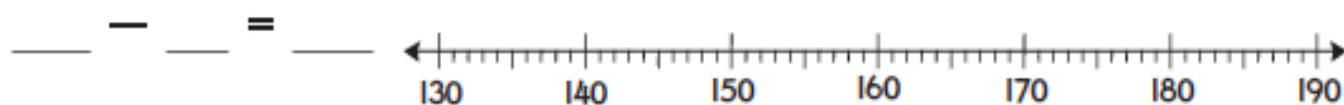
Round 1



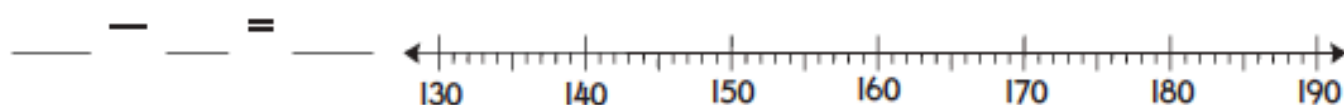
Round 2



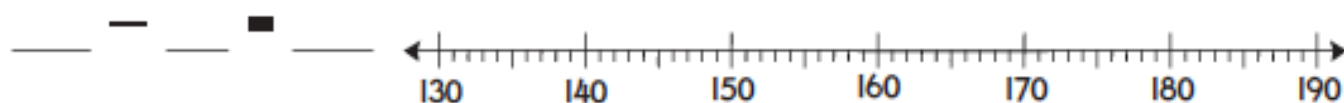
Round 3



Round 4

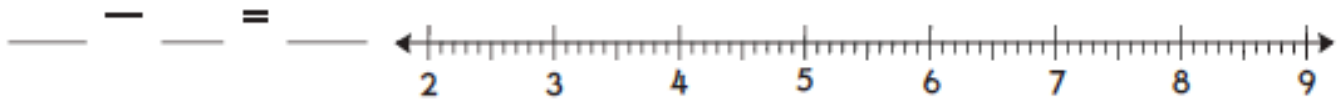


Round 5

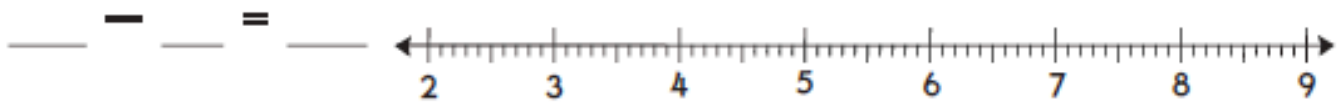


Jump Back Again

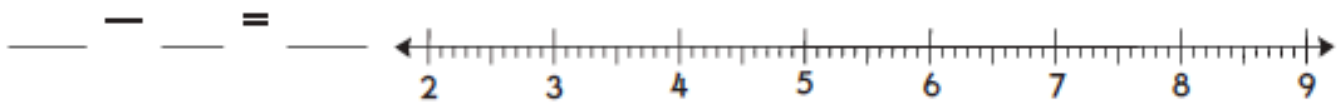
Round 1



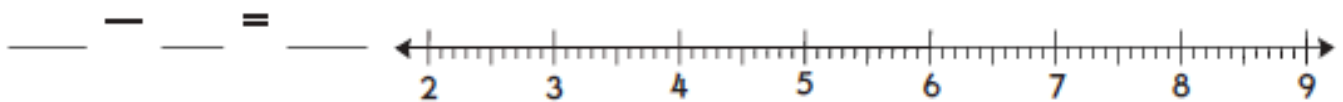
Round 2



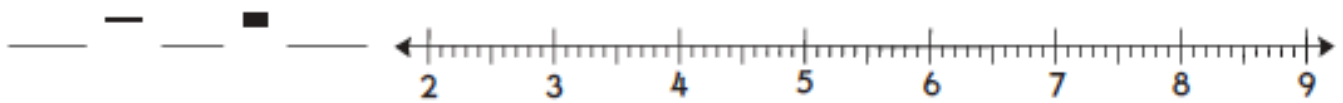
Round 3



Round 4



Round 5



Up or Down

Adjusting numbers to subtract

2 or 3 players

Purpose

In this game, the students are required to find the difference between two two-digit numbers. The students discover that changing both totals in the same way keeps the difference unchanged. This is an efficient mental strategy for subtraction, when the calculation involves bridging across a ten.

Materials

Each group of players will need

- An 'Up or Down' game board (page 34) as shown below.
- Two (2) number cubes made from blank wooden cubes. One cube should show the numerals 92, 82, 72, 62, 52, and 42. The other cube should show 17, 27, 37, 17, 27, and 37.

Each player will need

- Fifteen (15) counters (a different color for each player).

| Up or Down | | | | | | | | | |
|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 90 - 15 | 80 - 15 | 70 - 15 | 60 - 15 | 50 - 15 | 40 - 15 | 90 - 20 | 80 - 20 | 70 - 20 | 60 - 20 |
| 90 - 25 | 80 - 25 | 70 - 25 | 60 - 25 | 50 - 25 | 40 - 25 | 90 - 30 | 80 - 30 | 70 - 30 | 60 - 30 |
| 90 - 35 | 80 - 35 | 70 - 35 | 60 - 35 | 50 - 35 | 40 - 35 | 90 - 40 | 80 - 40 | 70 - 40 | 60 - 40 |
| 90 - 45 | 80 - 45 | 70 - 45 | 60 - 45 | 50 - 45 | 40 - 45 | 90 - 50 | 80 - 50 | 70 - 50 | 60 - 50 |
| 90 - 55 | 80 - 55 | 70 - 55 | 60 - 55 | 50 - 55 | 40 - 55 | 90 - 60 | 80 - 60 | 70 - 60 | 60 - 60 |
| 90 - 65 | 80 - 65 | 70 - 65 | 60 - 65 | 50 - 65 | 40 - 65 | 90 - 70 | 80 - 70 | 70 - 70 | 60 - 70 |
| 90 - 75 | 80 - 75 | 70 - 75 | 60 - 75 | 50 - 75 | 40 - 75 | 90 - 80 | 80 - 80 | 70 - 80 | 60 - 80 |
| 90 - 85 | 80 - 85 | 70 - 85 | 60 - 85 | 50 - 85 | 40 - 85 | 90 - 90 | 80 - 90 | 70 - 90 | 60 - 90 |
| 90 - 95 | 80 - 95 | 70 - 95 | 60 - 95 | 50 - 95 | 40 - 95 | 90 - 95 | 80 - 95 | 70 - 95 | 60 - 95 |

How to Play

The aim is to arrange three counters adjacently in a horizontal, vertical, or diagonal line.

- The first player rolls the number cubes.
- The player says the subtraction sentence represented by the cubes, then figures out and says an equivalent subtraction sentence.

Example: Reece rolls 42 and 17, and says, 42 take away 17 is the same as 40 take away 15 or 45 take away 20.

- The player states the difference before claiming a corresponding space on the game board by covering it with a counter. If both choices are unavailable, the player misses a turn.

Example: Reece says, The answer is 25, and claims 40 - 15 or 45 - 20 on the game board.

- The other player(s) has a turn.
- The first player to make a line of three adjacent counters is the winner.

Reading the Research

Research shows that children need many different kinds of number experiences to help them deal with real-life situations. It is important that they work regularly with a variety of number representations, including a counting model, a linear model such as a number line, a place-value model and a quantity model (Irons, 2002).

Before the Game

Draw a number line like that shown (right) on an overhead transparency. Invite a volunteer to roll the number cubes and mark the location of the numbers on the line. This number line shows that 42 and 17 was rolled. Place another blank



transparency over the number line. Draw a loop to show the difference between the two numbers. Say, *If we can't quickly calculate the difference, it is sometimes easier to change the two numbers.*

Slide the loop along the number line until the ends are resting on 40 and 15, and ask, *Have I changed the loop or difference?* (No.) *Is it easier to calculate $40 - 15$ in our heads?* (Yes.) Slide the loop in the other direction until the ends are resting on 45 and 20. Again ask, *Is it easier to calculate $45 - 20$?* (Yes.)



During the Game

Encourage the students to explain the strategy they use to find the answers. Different players will use different strategies. For example, after figuring out that $72 - 37$ is the same as $70 - 35$, the following players gave these explanations:

Grace: *I subtracted 30 then another 5. The answer is 35.*

Grant: *I just knew that double 35 is 70, so 70 take away 35 must be 35.*

Gabby: *I started with 35 and added 5 to get 40 and another 30 to get 70. The difference is $5 + 30$.*

After the Game

Lead a discussion about the strategy introduced in the game. Ask, *Did you find this strategy easy (or difficult) to use? Why was it easy (or difficult)? Did you prefer to adjust the numbers down or up? Why?*

Up or Down Again

| | | | | | | |
|----|----|----|----|----|----|----|
| | | | | | | |
| 65 | 45 | 35 | 25 | 15 | 5 | |
| 65 | 55 | 45 | 35 | 25 | 15 | 5 |
| 65 | 55 | 45 | 35 | 25 | 15 | 5 |
| 75 | 65 | 55 | 45 | 35 | 25 | 15 |
| 5 | 5 | 5 | 5 | 5 | 5 | 5 |

Beyond the Game

- The students can play 'Up or Down' using a different pair of cubes. On the faces of one cube, write the numerals 18, 28, 38, 18, 28, and 38. The other cube should show 93, 83, 73, 63, 53, and 43.
- The students can play the same game using a different game board. Give them a copy of 'Up or Down Again' shown on page 35 (illustrated). This time, the students verbalize the equivalent number sentence and cover the answer.

| | | | | |
|-------|-------|-------|-------|-------|
| 90-15 | 95-20 | 90-25 | 95-30 | 90-35 |
| 80-15 | 85-20 | 80-25 | 85-30 | 80-35 |
| 70-15 | 75-20 | 70-25 | 75-30 | 70-35 |
| 60-15 | 65-20 | 60-25 | 65-30 | 60-35 |
| 50-15 | 55-20 | 50-25 | 55-30 | 50-35 |
| 40-15 | 45-20 | 40-25 | 45-30 | 40-35 |

| | | | | |
|----|----|----|----|----|
| 75 | 75 | 65 | 65 | 55 |
| 65 | 65 | 55 | 55 | 45 |
| 55 | 55 | 45 | 45 | 35 |
| 45 | 45 | 35 | 35 | 25 |
| 35 | 35 | 25 | 25 | 15 |
| 25 | 25 | 15 | 15 | 5 |