



Early Geometry Concepts

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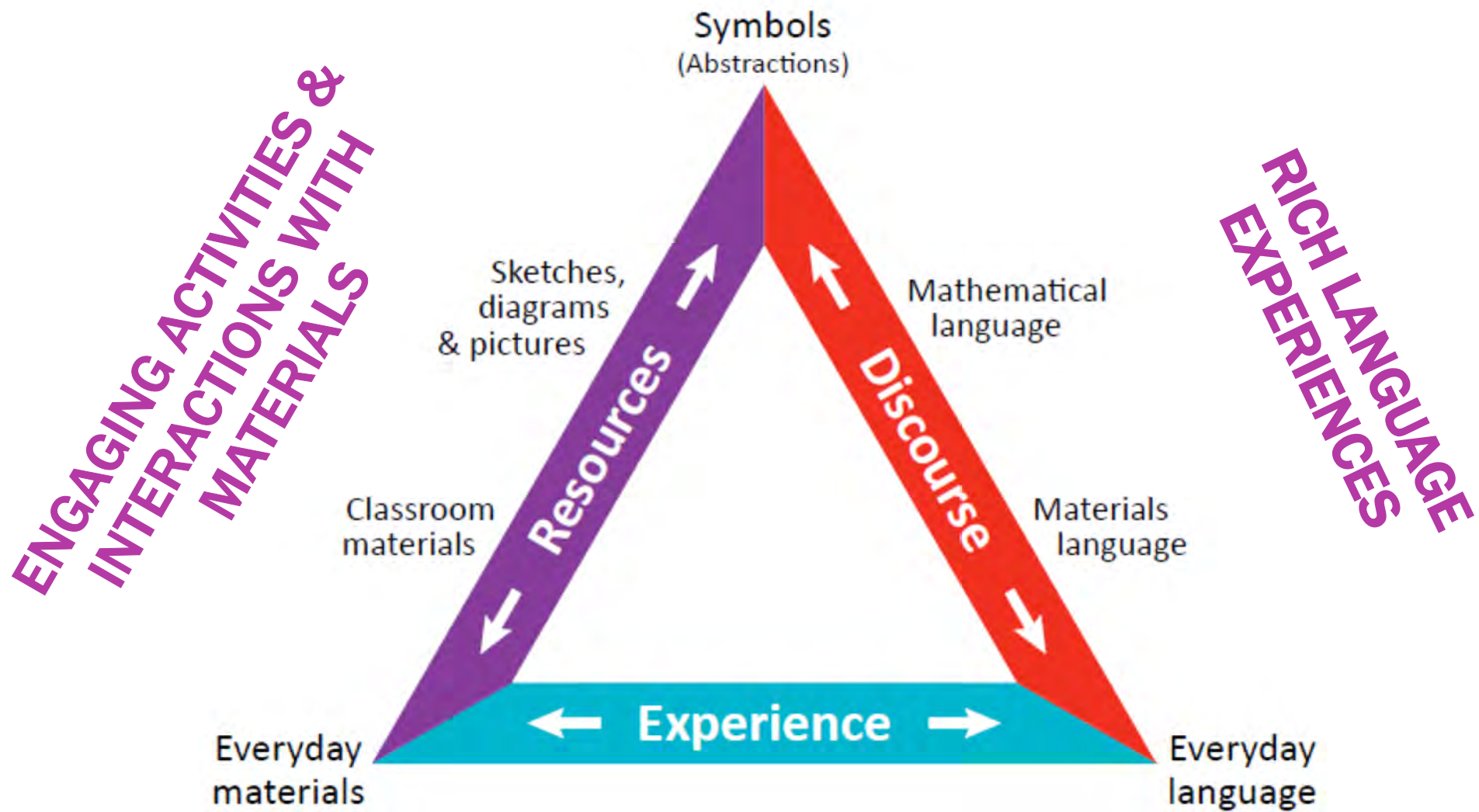
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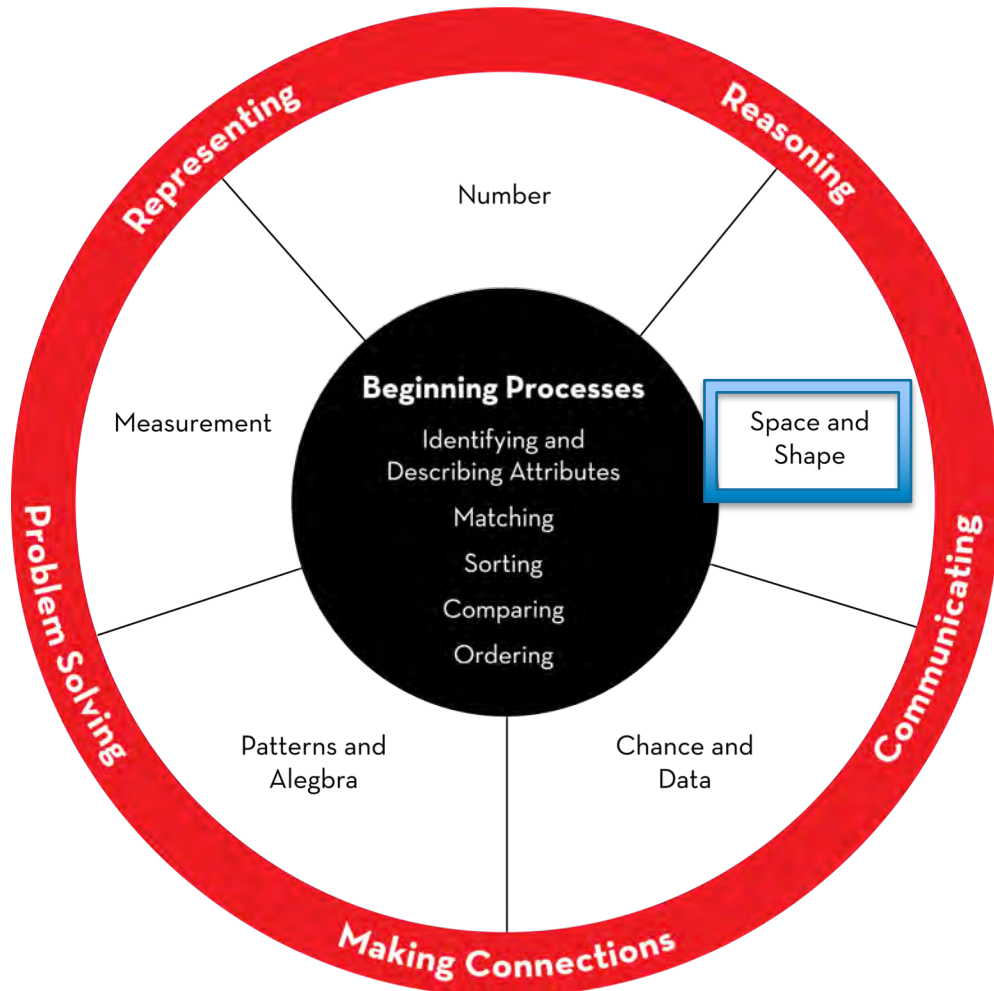
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*Adapted from Ed Rathmell
and Joseph Payne.

Pre-requisite Skills: Another Progression



Early Childhood Mathematics Framework

Irons, 2007

Key Components of Executive Function

Cognitive flexibility

- Use a variety of strategies to solve a problem
- Switch attention from one part of a problem to another

How many ways can you sort these objects?



Banse, Clements, Sarama, Day-Hess, Joswick. (2021).

Key Components of Executive Function

Working memory, managing incoming information

- Maintain
- Update
- Integrate



Pngkey.com

There are 9 leaves.
2 leaves blow away.
How many leaves are left?

Banse, Clements, Sarama, Day-Hess, Joswick. (2021).

Key Components of Executive Function

Inhibitory Control

- Regulation of impulses and suppression of automatic responses
- May be behavioral, cognitive, or both (often difficult to distinguish)

- Behavioral – physical actions and body support task completion



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- Cognitive – mental actions support task completion; suppressing automatic responses

Banse, Clements, Sarama, Day-Hess, Joswick. (2021).

Choosing the Best

- Engaging activities that begin with concrete materials, move to pictorial, and then to symbolic
- A progression of language from student language to materials language to mathematical, and then symbolic
- A progression of activities with beginning processes
- Activities that promote executive function



Why Study Geometry in School?

- Practical application
 - Why is the hexagon everywhere?
 - Why are manhole covers round?
- Develops spatial thinking, a factor of intelligence and an important predictor of future careers, especially in scientific research, engineering and the arts.



Vyas, 2018

Ivie & Embreston, 2010

For Young Learners, Spatial Perception Involves. . .

Eye-motor coordination – the ability to coordinate vision and body movement.

- Gross motor – obstacle course, skipping, and more
- Fine motor – pencil, rulers, stringing beads, working with a computer, and more



Del Grande, 1993

For Young Learners, Spatial Perception Involves. . .

Figure-ground perception – the ability to distinguish foreground from background and identifying a figure against a complex background.

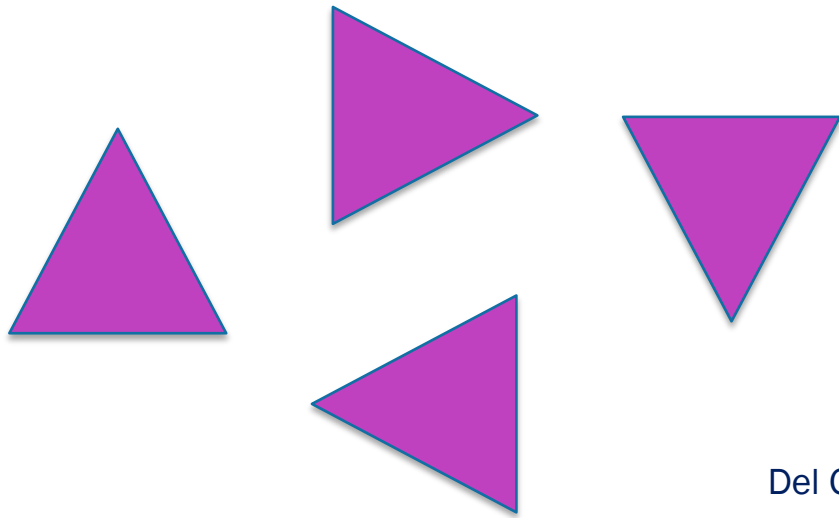


Del Grande, 1993

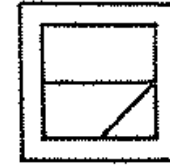


For Young Learners, Spatial Perception Involves...

Perceptual constancy – the ability to recognize figures or objects in space, regardless of size, position, or orientation.



Del Grande, 1993



- 3 figures below can be fitted together to make a square like the one in the box
- Mark the pieces with an X



For Young Learners, Spatial Perception Involves. . .

Position-in-space perception – the ability to recognize how an object in space is related to themselves and how an object has changed positions.

- Interpretation of letters and numerals is dependent upon the relationship to the top and sides of the page.

p, q, b, d, 6, 9



Del Grande, 1993

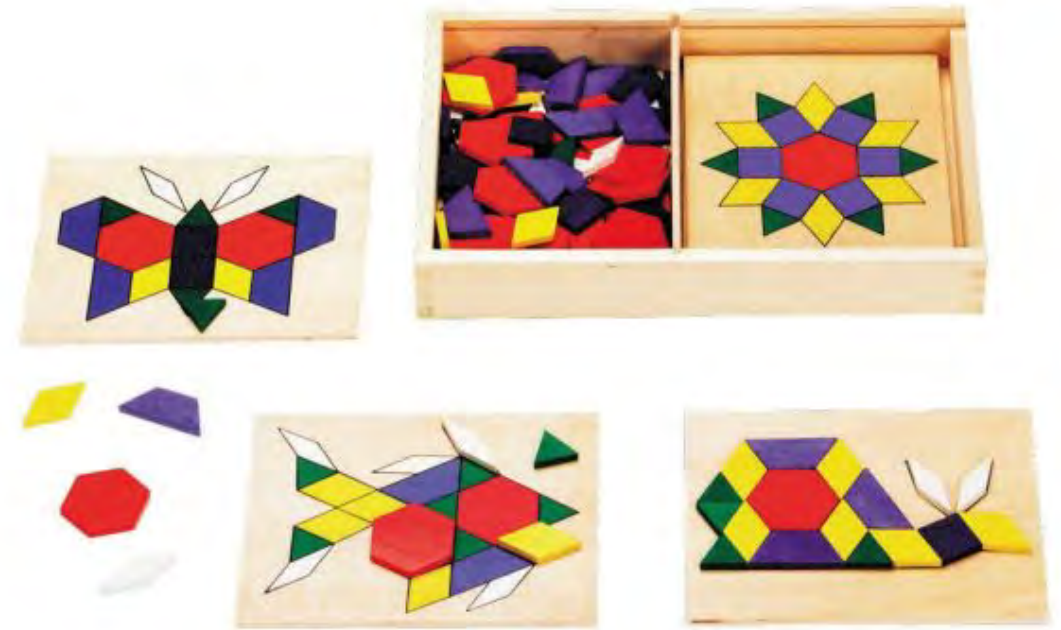
For Young Learners, Spatial Perception Involves. . .

Perception of spatial relationships

– the ability to see the two or more objects in relation to each other or to oneself.

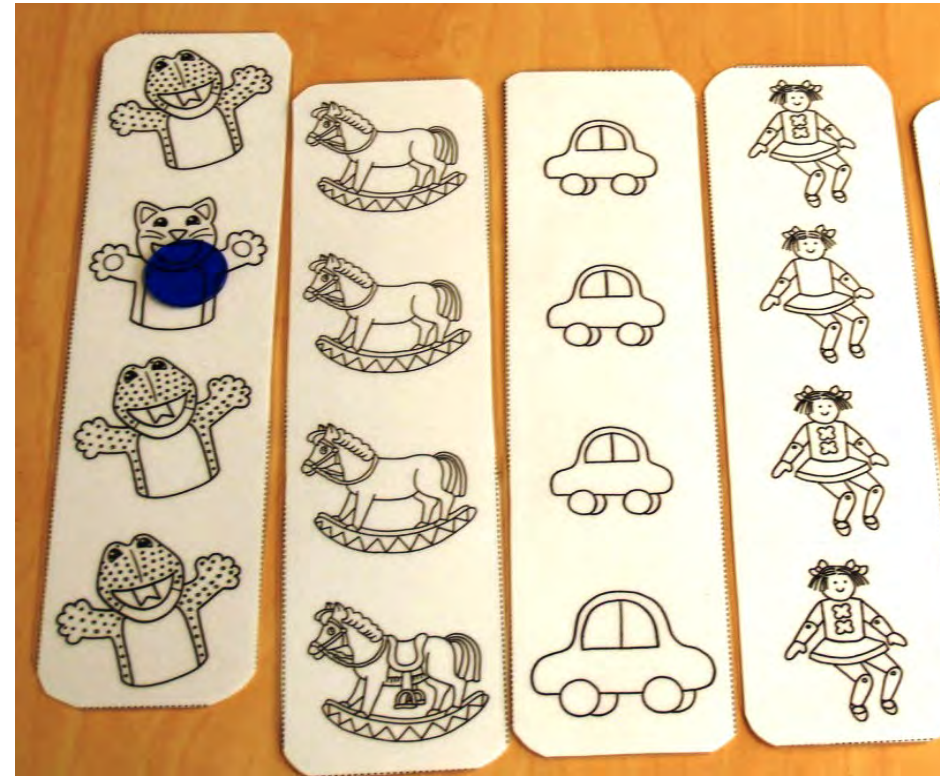


Del Grande, 1993



For Young Learners, Spatial Perception Involves. . .

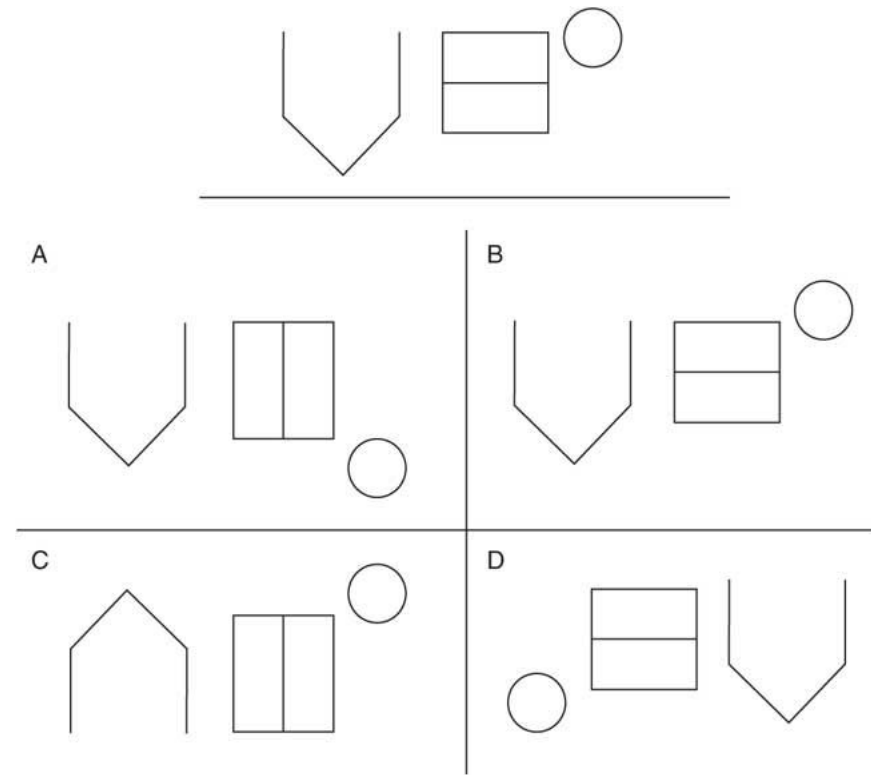
Visual discrimination – the ability to identify similarities and differences in an object's characteristics.



Del Grande, 1993

For Young Learners, Spatial Perception Involves. . .

Visual memory – the ability to recall objects and the characteristics of objects that are no longer visible.



Benton visual retention test

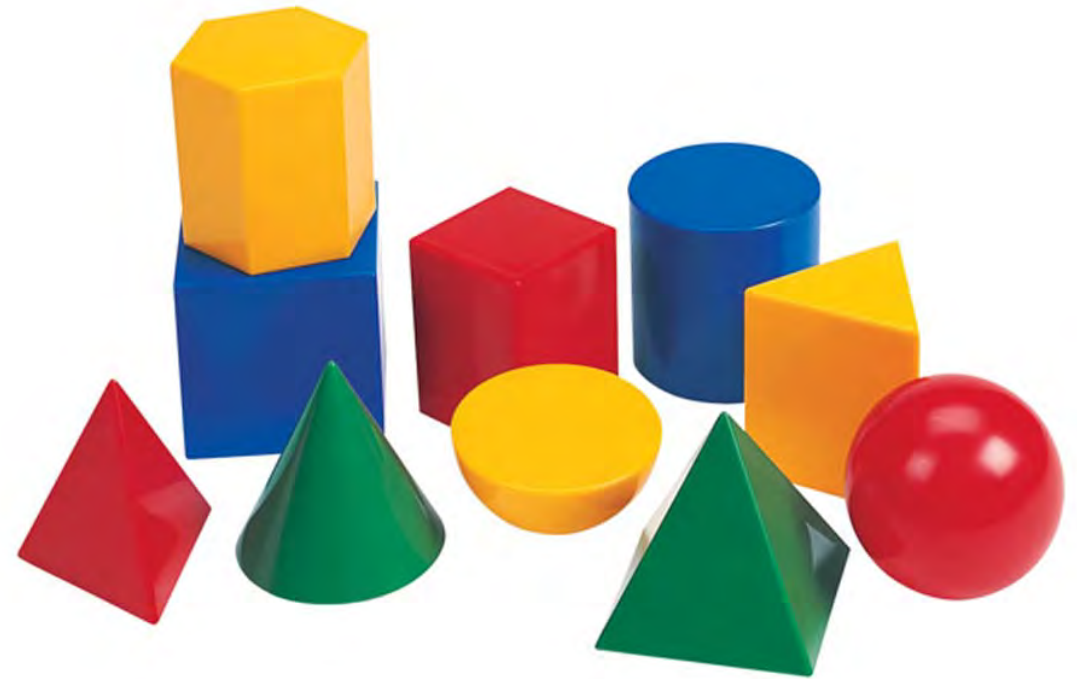
Del Grande, 1993

3-D Objects: Their Everyday World!



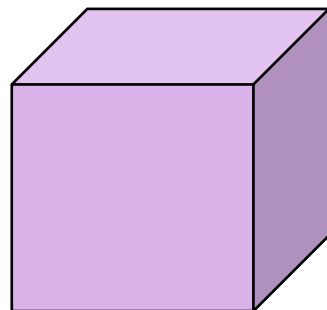
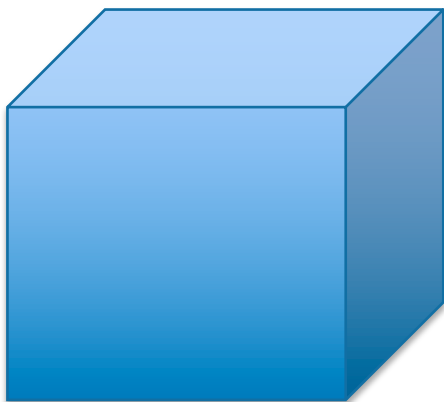
3D Objects for Young Learners

- Prism
- Pyramid
- Cone
- Cylinder
- Sphere
- Cube

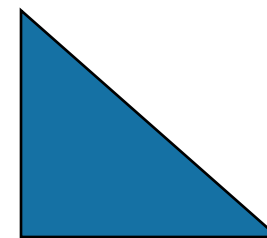
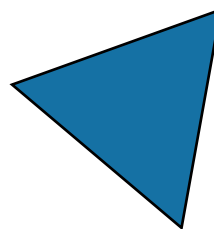


Critical Attributes: 3D *and* 2D Shapes

An important aspect of geometry for early learners is that geometrical shapes possess **critical attributes-must haves**.



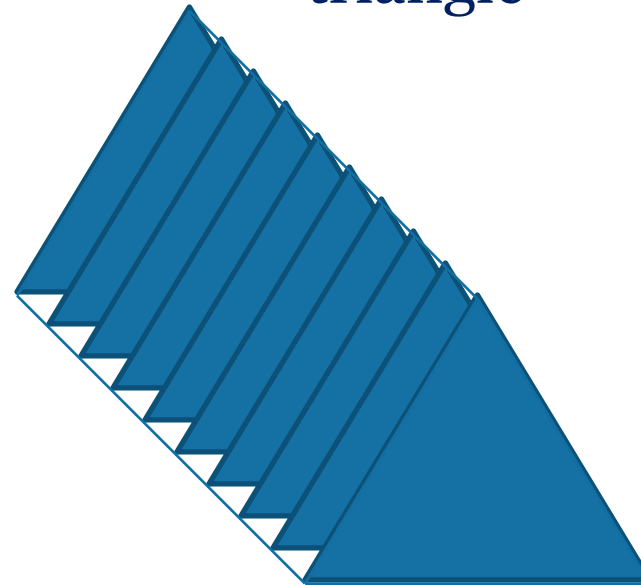
- A cube might be blue or purple, big or little, but it must have six faces.
- A triangle might have different orientations, but it must have three sides and three corners.



Prisms

Prisms are made from congruent shapes.

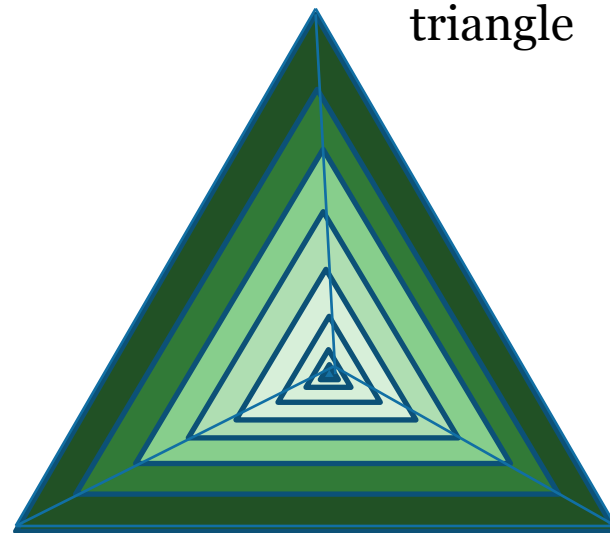
triangle



triangular prism

Pyramids

Pyramids are similar shapes, getting smaller toward the vertex.

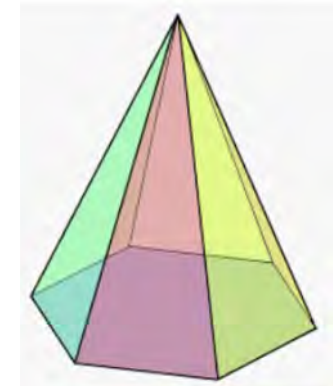
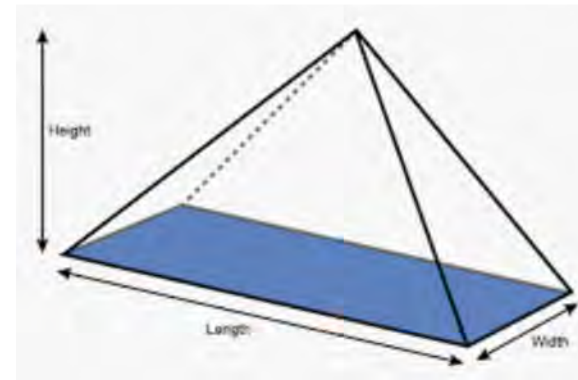


triangle

triangular-based
pyramid

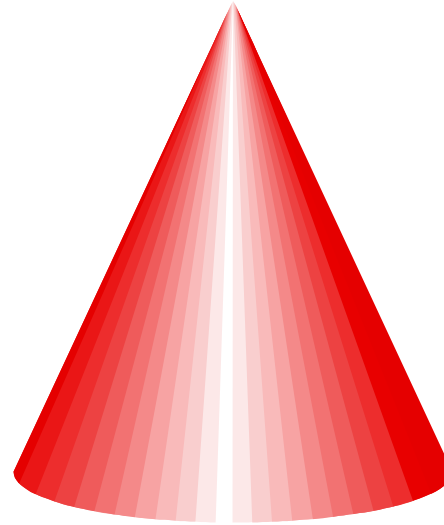
Pyramids

- Only one base
- All other faces are triangular
- Common vertex (apex)
- Pyramids are named according to the shape of their base:
 - Triangular-based pyramid
 - Square-based pyramid
 - Rectangular-based pyramid
 - Hexagonal-based pyramid



Cones

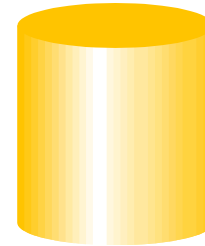
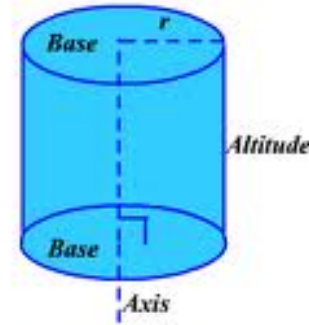
- Related to a pyramid
- Circular base
- A vertex (apex)
- A curved surface from circular base to vertex
- Height found by a perpendicular line from apex to the base plane



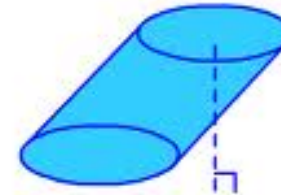
Cylinders

- Related to a prism (like cone is to a pyramid)
- Has two congruent circular and parallel bases
- A curved surface linking the two bases
- Height found by drawing a perpendicular line from the top base plane to the bottom base plane

Right Cylinder

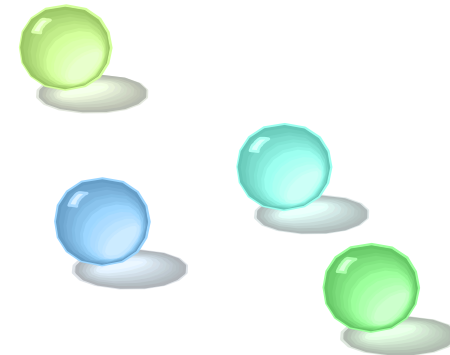
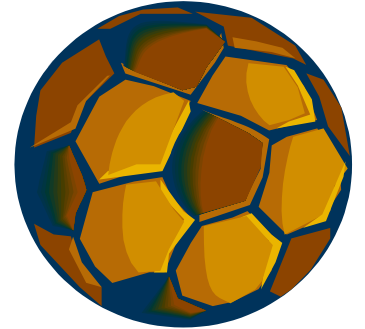


Oblique Cylinder



Spheres

- Completely curved surface
- No edges
- No vertices
- Same distance from center to any point on its surface



Cubes

- How would you want your students to describe a cube?
- What attributes would you want them to notice?



Attributes of 3D Objects

The **characteristics, attributes, or features** are more important than the names of the objects and shapes.

- similarities and differences
- straight and curved surfaces or faces
- roll, stack, number of faces, corners, edges
- number of sides and angles



Analytical Approach to 3D

Emphasizes the **attributes** of the object.

- Does it roll, stack, or both?
- Same number of faces, edges, corners?



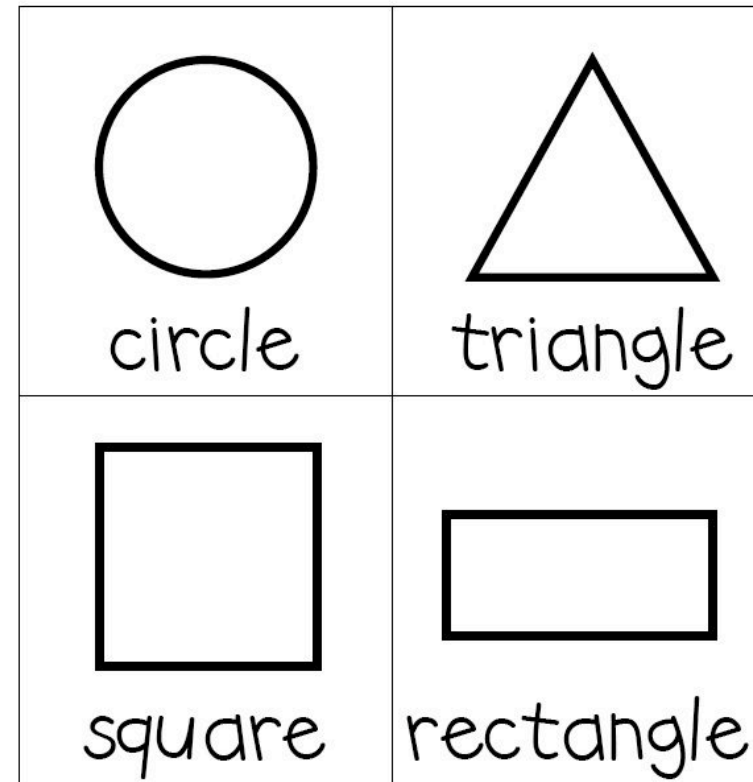
Holistic Approach to 3D

Involves building **families** of objects with geometric similarity



2D Shapes for Young Learners

Relating 2D shapes to 3D objects



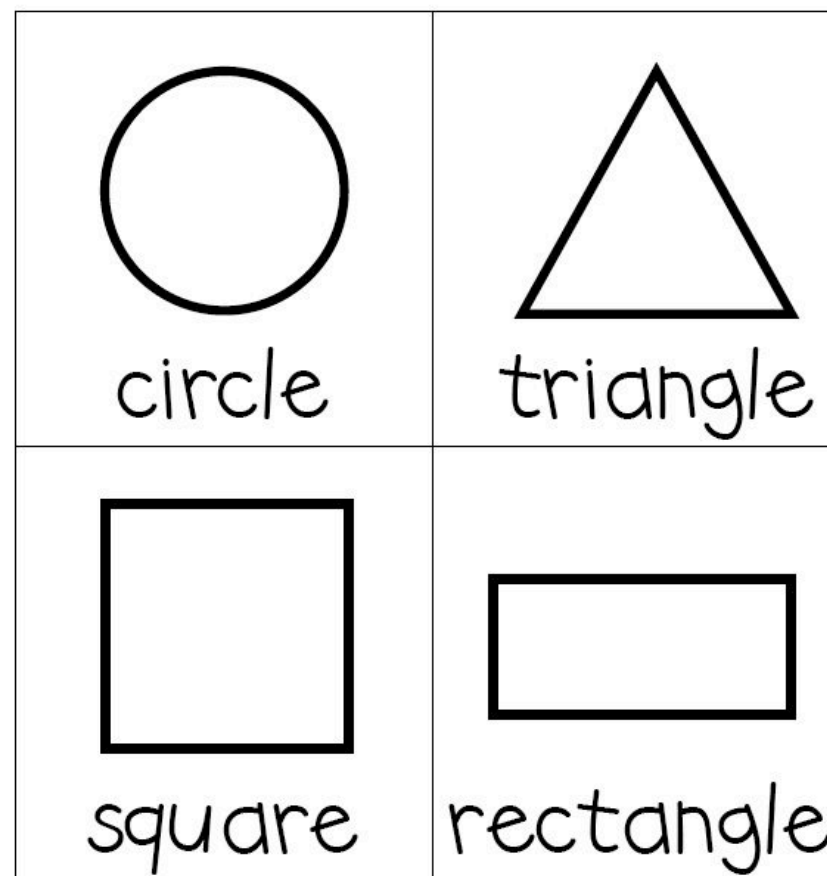
3D to 2D Understanding



2D Shapes for Young Learners

Attributes:

- No thickness
- Are flat
- Corners
- Sides

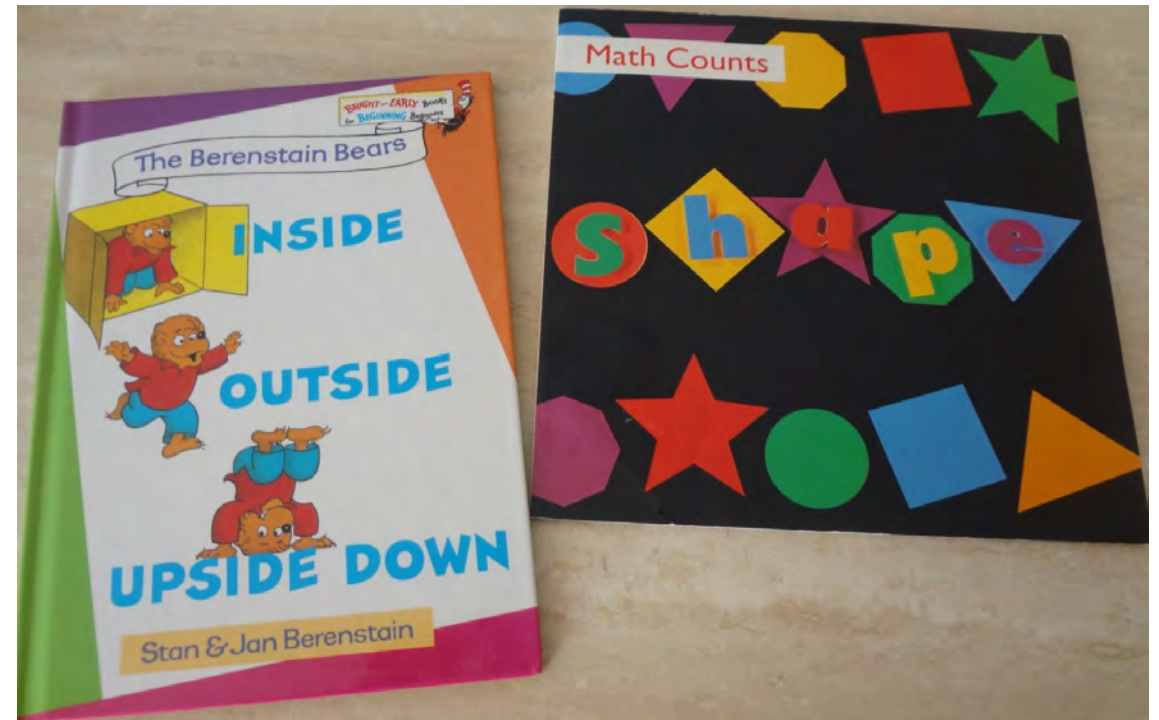


Critical and Non-critical Properties

- Critical properties are the ones a shape must have
- Non-critical properties can confuse students
- Many students include non-critical attributes in their definitions
- Many students develop their own definitions through observation and deduction

Beware of Misconceptions

More than 60 percent of commercial geometry books for children have incorrect representation and language for three-dimensional objects and two-dimensional shapes.



Food for Thought

“Students do misunderstand, but it is seldom because they cannot understand, most often it is because they understand something else.” (Tripp, D. 1993)

- Students can get the right answers for the wrong reasons and the wrong answers for the right reasons.
- In all cases asking students what they think is important.
- Good questions and thoughtfully chosen tasks can help the teacher to know which is which.



Thank you!!! Any questions?

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